

Ay 7A – Fall 2009
Section Worksheet 9
And I’m Free, Free Fallin’ – The Jeans Criterion

Stars are born from the gravitational collapse of clouds of interstellar gas. But what determines whether or not a given cloud will collapse? Why aren’t all clouds of gas in the interstellar medium (ISM) of the Galaxy undergoing gravitational collapse and forming stars? In this problem we will examine the necessary conditions for collapse to occur.

1. If we have a cloud of gas of mass M and initial mass density ρ , what is the cloud’s average potential energy, $\langle U \rangle$, in terms of the variables given and fundamental constants?

2. In a gas cloud, the kinetic energy is due to the random motions of the N particles that make up the cloud. Our cloud has a temperature T and a mean molecular weight μ . Estimate the average kinetic energy, $\langle K \rangle$, of the cloud in terms of the variables given and fundamental constants.

3. Recall the Virial Theorem:

$$\langle U \rangle = -2\langle K \rangle$$

If this equality holds, we say the system is in “virial equilibrium”. However, if the force of gravity in the cloud is greater than the gas pressure force (i.e., the kinetic energy), the system will collapse. Thus collapse will occur if

$$|\langle U \rangle| > |-2\langle K \rangle|$$

Plug your expressions for $\langle U \rangle$ and $\langle K \rangle$ into this inequality and solve for mass (and call it M_J).

4. The critical mass you derived above, the **Jeans mass**¹, is the minimum mass needed for a cloud of gas to undergo spontaneous gravitational collapse. Typical diffuse clouds in the ISM have masses ranging from 1 to 100 M_{\odot} . They have typical temperatures and number densities of $T \sim 100$ K and $n \sim 50$ cm^{-3} . Assuming that such clouds are composed entirely of atomic hydrogen, would you expect them to be sites of star formation?

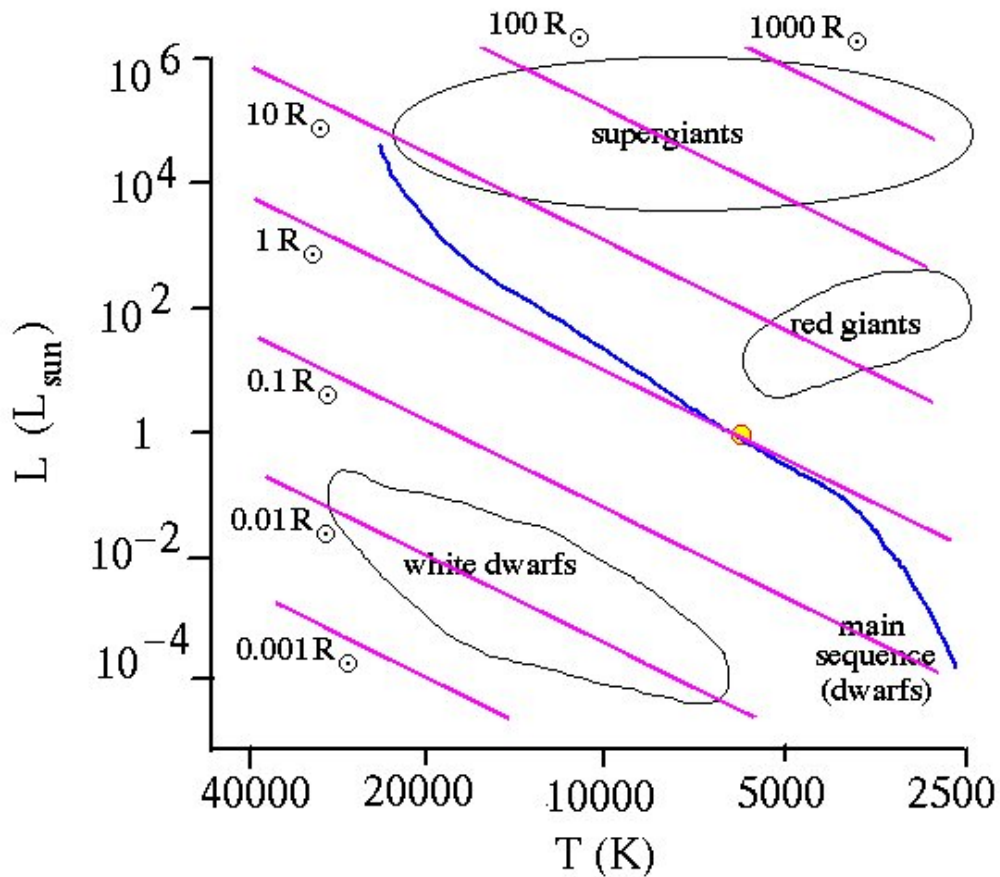


Figure 1: A Hertzsprung-Russell diagram with some actual numbers on it. The horizontal axis is surface (or “effective”) temperature, T_{eff} , which has a one-to-one correspondence with color (i.e., peak wavelength) through Wien’s Law. The Sun is marked by the small circle of course.

¹Named after the British physicist Sir James Jeans who was the first to consider this problem.